Foundation for Success

Unified International
Mathematics Olympiad

## UNIFIED INTERNATIONAL MATHEMATICS OLYMPIAD



KEY

| 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| B | B | D | B | A | D | A | C | C | A |
| 11 | 12 | 13 | 14 | 15 | 16 | 17 | 18 | 19 | 20 |
| B | B | C | B | C | B | D | C | D | C |
| 21 | 22 | 23 | 24 | 25 | 26 | 27 | 28 | 29 | 30 |
| A | A | B | B | C | A | A | A | B | B |
| 31 | 32 | 33 | 34 | 35 | 36 | 37 | 38 | 39 | 40 |
| B | C | A | C | B | C | D | C | B | A |
| 41 | 42 | 43 | 44 | 45 | 46 | 47 | 48 | 49 | 50 |
| A | A | B | D | C | C | B | D | C | D |

## EXPLANATIONS

## MATHEMATICS

1. (B) By removing block K there will be no change in perimeter.
2. (B) To convert $1 \frac{4}{5}$ to an improper fraction:

Number of fifths from the whole number part (1) $=1 \times 5=5$ fifths Number of fifths from the fractional part $\frac{4}{5}=4$ fifths Total fifths $=5+4=9$

Therefore, the correct answer is 9 .
03. (D)

| 3 | 2145 |
| ---: | ---: |
| 5 | 715 |
| 11 | 143 |
|  | 13 |

$2145=3 \times 5 \times 11 \times 13$
$(3,5) ;(11,13)$ are twin primes,
i.e., $P$ and $R$ are the required twin primes.
04. (B) 1 complete turn have 4 right angle
$\therefore \quad 2 \frac{1}{2}$ complete turn $=4+4+2=10$
05. (A) Product of $999999999 \times 888888888$ Multiply only the last 3-digits of each $999 \times 888=887112$

The digit in the hundreds place is 1.
06. (D) The time at which the movie ended = 8: 23 p.m.

Duration of the movie $=2 \mathrm{~h} 16 \mathrm{~min}$
$\therefore \quad$ The time at which the movie began = 8: 23 p.m. -2 h $16 \mathrm{~min}=6: 07$ p.m.
07. (A) The product of two even numbers is an even number. An even number can be divided into two equal parts with no remainder.
08. (C) Quantity of water in Tank B and Tank C = $90 l$

Quantity of water in Tank A and Tank C = $87 l$

Quantity of water in Tank $A=43 l$
$\Rightarrow$ Quantity of water in Tank
$C=(87-43) l=44 l$
and quantity of water in Tank B
$=90 l-44 l=46 l$
$\therefore \quad$ Total quantity of water in the three tanks
$=(43+46+44) l$
$=133 l$
$\Rightarrow \frac{1}{7}$ of the total quantity of water
$=\frac{1}{7} \times 133 l=19 l$
09. (C) $(3456 \times 2=6912)$
10. (A) Compare the digits at the same place value, which is the units digit in this case. The units digit is 8 in 345,678 and 9 in 345,679 .
11. (B) $A+B+45896=96023+B$
$A=96023-45896$
$=50127$
12. (B) Option (A) : $C-X=100-10$
$=90=$ XC (Correct)
Option $(B): X I-I X=(10+1)-(10-1)$
$=11-9=2 X X$ (Wrong)
Option (C) : DC - C = 500 + 100-100
$=500=\mathrm{D}$ (Correct)
Option (D) : LXI - LIX = [50+ $10+1]-[50$
$+(10-1)]=61-59=2=1 I$ (Correct)
13. (C) $777 \div 21=37$
14. (B) Equilateral triangle is a polygon.
15. (C) $4 \times 8 \times 12 \times 16 \times 20 \times 24$
16. (B) The number of ways we can combine the weights to get 2 kg
$1 \mathrm{~kg}+500 \mathrm{~g}+500 \mathrm{~g}=2 \mathrm{~kg}$
$1 \mathrm{~kg}+500 \mathrm{~g}+250 \mathrm{~g}+250=2 \mathrm{~kg}$
$1 \mathrm{~kg}+500 \mathrm{~g}+250 \mathrm{~g}+100 \mathrm{~g}+100 \mathrm{~g}+50 \mathrm{~g}$
$=2 \mathrm{~kg}$
In 3 different ways we can combine the weights
17. (D) 103 is not divisible by 3 but remaining options all are divisible by 3.
$4 4 \longdiv { 1 3 }$
18. (C) $\frac{-3346}{1067}$

Hence, missing number is (D)
19. (D) $41-12-12=18 \mathrm{~cm}$
$18 \div 2=9 \mathrm{~cm}$
The breadth is 9 cm
$12 \times 9=108 \mathrm{~cm}^{2}$
The area is $108 \mathrm{~cm}^{2}$.
20. (C) $4020 \mathrm{ml}+4530 \mathrm{ml}$
$=8550 \mathrm{ml}=8 l 550 \mathrm{ml}$
21. (A) $48=3 \times 16$ is a multiple of 16 $64=4 \times 16$ is a multiple of 16
$80=5 \times 16$ is a multiple of 16
$44=2 \times 2 \times 11$ is not a multiple of 16
$42=6 \times 7$ is a not a multiple of 16
$66=3 \times 2 \times 11$ is not a multiple of 16
$86=2 \times 43$ is not a multiple of 16
$46=2 \times 23$ is not a multiple of 16
$68=2 \times 2 \times 17$ is a multiple of 16
$88=2 \times 2 \times 2 \times 11$ is not a multiple of 16.
22. (A) $\frac{3}{8}$ lies between $J$ and $L$.
23. (B) $2 \times 36 \times 3=12 \times 1 \times 18$
$=9 \times \underline{6} \times 4$.
So, the missing number is 6 .
24. (B) Million is the seventh place in the international system of numeration.
25. (C)


2 units $\rightarrow 555 \mathrm{~cm}-135 \mathrm{~cm}$
$=420 \mathrm{~cm}$
1 unit $\rightarrow 420 \mathrm{~cm} \div 2$
$=210 \mathrm{~cm}$
$210 \mathrm{~cm}+135 \mathrm{~cm}=345 \mathrm{~cm}$
26. (A) $X L I X=49, L X X I=71, X C I=91, X L I I=42$,
$X C V=95$
27. (A) 47,59, 29, 31 are prime numbers and have only two factors.
28. (A) On Monday.
29. (B) length $=2+2+2+2=8 \mathrm{~cm}$

Breadth $=4 \mathrm{~cm}$
Perimeter $=2(l+b)=2 \times 12 \mathrm{~cm}=24 \mathrm{~cm}$

30. (B) $5 \times 25 \mathrm{~min}=125 \mathrm{~min}$
$=120 \mathrm{~min}+5 \mathrm{in}$
$=2 \mathrm{~h} 5 \mathrm{~min}$
She takes 2 h 5 min to sew 5 dresses.
8.30 a.m. $\rightarrow 8$ h 30 min
$8 \mathrm{~h} 30 \mathrm{~min}+2 \mathrm{~h} 5 \mathrm{~min}=10 \mathrm{~h} 35 \mathrm{~min}$
$\rightarrow 10.35$ a.m.
She will have sewn 5 dresses at 10.35 a.m.
31. (B) The line segments formed are $A B, B D$, $C D, A C, A D$ and $C B$, which are 6 in number.
32. (C) Sally is busy for $8+4=12$ hours. The remaining time is $24-12=12$ hours.

Fraction $=\frac{\text { Remaining Time }}{\text { Total Time }}=\frac{12}{24}=\frac{1}{2}$

So, the correct answer is (C) $\frac{1}{2}$.
33. (A) Inner square $(P)=24 \mathrm{~cm}$
$l=\frac{24 \mathrm{~cm}}{4}=6 \mathrm{~cm}$

34. (C) 3: 30 cannot be taken as thirteen minutes past six, as 30 minutes passed after 3
35. (B) Correct answer is 5100 m

Total distance $=2 \mathrm{~km}+3000 \mathrm{~m}+10,000$ $\mathrm{cm}=2000 \mathrm{~m}+3000 \mathrm{~m}+100 \mathrm{~m}=5100 \mathrm{~m}$

## REASONING

36. (C)

37. (D) ANT , BAT , CAT, DOT, EAT

A14T, B1T, C1T, D15T, E1T
38. (C) The last two digits interchange the position in an order also first and last two digits as a pair again interchange the position.

H U N D R E D
39. (B) $-1 \begin{array}{llllll}+1 & -1 & +1 & -1 & +1 & -1\end{array}$

40. (A) 5
(Words, Tokyo, Writer, Hippo, Artist)
41. (A)


Hence, the number of $\square$ shapes is 18 .

43. (B) The sequence is number of lines.

1, 2, 3, 4, 5
i.e., R, P, T, Q, S
44. (D)

45. (C) In option (C) only there are similar in outer image and inner image.

## CRITICAL THINKING

46. (C)

47. (B)

| 1 | 2 | 3 | 4 | 5 | 6 |
| :---: | :---: | :---: | :---: | :---: | :---: |
| 20 | 21 | 22 | 23 | 24 | 7 |
| 19 | 32 | 33 | 34 | 25 | 8 |
| 18 | 31 | 36 | 35 | 26 | 9 |
| 17 | 30 | 29 | 28 | 27 | 10 |
| 16 | 15 | 14 | 13 | 12 | 11 |

48. (D) All pairs can pass through the cutouts.
49. (C) The correct answer is: C. The middle point is always less bumpy as, like a seesaw, the middle moves the least.
50. (D) Both the statements I and II are effects of independent causes.
